Solution

1.

$$Av = \frac{1/jC\omega}{R + 1/jC\omega} = \frac{1}{1 + jRC\omega} = \frac{1}{1 + j\omega/\omega_0}$$

$$|Av| = \frac{1}{\sqrt{1 + (\frac{\omega}{\omega_0})^2}} = \frac{1}{\sqrt{1 + \left(\frac{f}{fc}\right)^2}}$$

2. $\omega_0 = RC = 2\pi fc \quad \Rightarrow \quad fc = 1/2\pi RC = 7{,}96$ kHz (fréquence de coupure)

3. à la fréquence de coupure : f = fc

$$|Av| = \frac{Us}{Ue} = \frac{1}{\sqrt{1+\left(\frac{f}{fc}\right)^2}} = \frac{1}{\sqrt{1+(1)^2}} = \frac{1}{\sqrt{2}} \qquad \mathbf{Us = \frac{10}{\sqrt{2}} = 7{,}07V}$$

$$G(dB) = 20\log|Av| = 20\log\frac{1}{\sqrt{2}} \qquad \mathbf{G(dB) = -3dB}$$

$$\varphi = -\text{Arctg}\,\omega/\omega_0 = -\text{Arctg}1 \qquad \mathbf{\varphi = -45^\circ}$$

4. $$G(dB) = 20\log|Av| = 20\log\frac{1}{\sqrt{1+\left(\frac{\omega}{\omega_0}\right)^2}} = 20\log 1 - 10\log(1 + (\omega/\omega_0)^2)$$

$$G(dB) = -10\log(1 + (\omega/\omega_0)^2) = -10\log(1 + (f/fc)^2)$$

$$\varphi = -\text{Arctg}\,\omega/\omega_0 = -\text{Arctg}\,f/fc$$

	f(Hz)	Us(V)	Av(dB)	φ (degré)
fc	7957,75	7,07	-3,01	-45,00
fc/10	795,77	9,95	-0,04	-5,71
fc/2	3978,87	8,94	-0,97	-26,57
2fc	15915,49	4,47	-6,99	-63,43
10fc	79577,47	1,00	-20,04	-84,29

5.